

300311(14)

B. E. (Third Semester) Examination, 2020

APR-MAY

(Old Scheme)

**(Chemical, Civil, Mechanical, Metallurgy,
Mining Engg. Branch)**

MATHEMATICS-III

Time Allowed : Three hours

Maximum Marks : 80

Minimum Pass Marks : 28

***Note : Part (a) carries 2 marks and it is compulsory.
Attempt any two parts from (b), (c) and (d) of
each unit.***

Unit-I

1. (a) If $f(x)$ is an even function in $(-l, l)$, then

the value of $b_n =$ -----.

2

(b) Obtain Fourier series for the function 7

$$f(x) = \begin{cases} \pi x, & 0 \leq x \leq 1 \\ \pi(2-x), & 1 \leq x \leq 2 \end{cases}$$

Deduce that :

$$\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots \infty = \frac{\pi^2}{8}$$

(c) Obtain a half range cosine series for 7

$$f(x) = \begin{cases} kx, & 0 \leq x \leq 1/2 \\ k(1-x), & 1/2 \leq x \leq 1 \end{cases}$$

Deduce the sum of the series.

$$\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots \infty$$

(d) Obtain the first three coefficients in the Fourier cosine series for y, where y is given in the following table : 7

x :	0	1	2	3	4	5
y :	4	8	15	7	6	2

Unit-II

2. (a) $L\{e^{2t} \sin t\} = \dots\dots\dots$ 2

(b) Evaluate : 7

(i) $\int_0^\infty e^{-t} \left(\frac{\cos at - \cos bt}{t} \right) dt$

(ii) $\int_0^\infty t e^{-3t} \sin t dt$

(c) Apply convolution theorem to evaluate : 7

$$L^{-1} \left[\frac{s}{(s^2 + a^2)^2} \right]$$

(d) Solve by the method of transforms, the equation : 7

$$y''' + 2y'' - y' - 2y = 0$$

given $y(0) = y'(0) = 0$ and $y''(0) = 6$.

Unit-III

3. (a) The complementary function of : 2

$$r^2 - 7s + 6t = e^{x+y} \text{ is } \dots\dots\dots$$

(b) Solve : 7

$$x^2(y-z)p + y^2(z-x)q = z^2(x-y)$$

(c) Solve : 7

$$(D^2 + 2DD' + D'^2 - 2D - 2D')Z = \sin(x+2y).$$

(d) Using the method of separation of variables, solve 7

$$\frac{\partial u}{\partial x} + 2\frac{\partial u}{\partial t} + u \text{ where } u(x,0) = 6e^{-3x}$$

Unit-IV

4. (a) Statement of Cauchy theorem. 2

(b) Evaluate $\int_C \frac{z^2 - z + 1}{z - 1} dz$, where C is the circle 7

(i) $|z| = 1$

(ii) $|z| = \frac{1}{2}$

(c) Find the Laurents expansion of $f(z) = \frac{7z-2}{(z+1)z(z-2)}$

in the region $1 < z+1 < 3$. 7

(d) Show that : 7

$$\int_0^{2\pi} \frac{\cos 2\theta d\theta}{1 - 2a \cos \theta + a^2} = \frac{2\pi a^2}{1 - a^2}, \quad (a^2 < 1).$$

Unit-V

5. (a) The mean of Binomial distribution with n observations and probability of success p is : 2

(i) pq

(ii) np

(iii) \sqrt{np}

(iv) \sqrt{pq}

(b) Find the moment generating function of the exponential distribution : 7

$$f(x) = \frac{1}{c} e^{-x/c}, \quad 0 \leq x \leq \infty, \quad c > 0.$$

Hence find its mean and S.D.

(c) Fit a Poisson distribution to the set of observations : 7

$x :$ 0 1 2 3 4

$y :$ 122 66 15 2 1

(d) In a normal distribution, 31% of the items are under 45 and 8% are over 64. Find the mean and S.D. of the distribution. 7